

Fig. 1. Scattering curves for ammonium and nitrogen.

values of  $\sin \theta/\lambda$ . This would be expected; electrons further away from the central nucleus seem to have little effect on the scattering factor at high values of  $\sin \theta/\lambda$ . This may be easily seen by reference to the atomic scattering factors in *International Tables* (1962), where atomic scattering factors for neutral and ionized atoms differ little at larger values of  $\sin \theta/\lambda$ . The errors in the present scattering factors are unknown but the calculation for  $\sin \theta/\lambda=0$  gives 9.998 and 10.001 for the values for the wave functions of Bernal (1953) and Bernal & Massey (1954) respectively compared with the correct value of 10.000, so the errors are probably in the third decimal place. This, of course, assumes that the N-H distances of 0.97 Å for which the wavefunctions were calculated is correct. The effect of a different N-H distance on the wavefunctions and hence on the scattering factors is not known.

Webb's (1965) figures were thought to be due to taking the abscissae of Banyard & March's (1961) curve to be in Å whereas they are in atomic units. However, a check calculation based on this gave moderate agreement at low values of  $\sin \theta/\lambda$  but very poor agreement at larger values of  $\sin \theta/\lambda$ . So this assumption cannot be entirely correct.

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**Chain structure of the orthorhombic modification of dicyclopentadienyl-lead containing bridging  $\pi$ -cyclopentadienyl rings.** By C. PANATTONI, G. BOMBIERI and U. CROATTO, *Centri Nazionali di Strutturistica Roentgenografica e Chimica delle Radiazioni e dei Radioelementi, Sezioni di Padova, Padova, Italy*

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### Introduction

The structure of  $\text{Pb}(\text{C}_5\text{H}_5)_2$  has aroused considerable interest. On the basis of infrared, nuclear magnetic resonance, ultraviolet spectra and dipole moment measurements

The scattering curves for ammonium found in the present investigation are very similar although there are differences of up to 10% in individual values. These differences are hardly likely to be important for most work but may cause errors in high accuracy work.

According to Banyard & March (1961) a comparison of the electron distribution curve for ammonium with that for methane suggests that the figures of Bernal & Massey (1954) are the more accurate and for this reason the scattering curve for ammonium taken from their figures is probably the best.

The scattering factor for ammonium has been determined experimentally from intensity measurements on ammonium chloride (Wyckoff & Armstrong, 1930). However, subsequently it has been shown, from infrared spectroscopy (Wagner & Hornig, 1950), neutron diffraction (Levy & Peterson, 1952) and electron diffraction (Vainshtein, 1964) that in the room temperature form of ammonium chloride, phase II, the ammonium is not rotating. It is at random in two orientations. Thus these calculated values cannot be compared with the experimental.

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In view of criticism by Dave, Evans & Wilkinson (1959), Fritz & Fischer (1961) later extended their earlier measurements of the infrared spectra and concluded that there exists a 'predominantly  $\pi$ -bonding with some additional  $\sigma$ -bonding between metal atoms and rings in dicyclopentadienyltin and probably also in the lead compound'.

### Experimental

We have prepared dicyclopentadienyl-lead by the Fischer & Grubert (1956) method. By sublimation in vacuum we have obtained two crystalline modifications which are very sensitive to exposure to air (Bombieri & Panattoni, 1966).

Modification 1 occurs as orthorhombic yellow needles, while modification 2, triclinic, has a prismatic habit of brown-yellow colour.

Very small crystals of modification 1 were enclosed in Lindemann capillaries in a nitrogen atmosphere. Multi-film Weissenberg methods with Cu  $K\alpha$  radiation and precession techniques with Mo  $K\alpha$  radiation were used to collect  $hk0$  and  $h0l$  intensity data, respectively. Intensities were measured with a photometer with a potentiometric recorder device and corrected for the Lorentz and polarization factors. On account of the uniform crystal cross-section and the very small dimensions of the crystal (less than 0.01 cm) absorption corrections were neglected. The unit cell containing four  $\text{Pb}(\text{C}_5\text{H}_5)_2$  molecules has orthorhombic symmetry and possesses the following dimensions:

$$a = 16.37 \pm 0.04, \quad b = 6.02 \pm 0.03, \quad c = 9.61 \pm 0.03 \text{ \AA}.$$

Observed density 2.361 g.cm<sup>-3</sup>, calculated density 2.370 g.cm<sup>-3</sup>. The observed systematic absences of  $k+l \neq 2n$  for  $\{0kl\}$  and  $h \neq 2n$  for  $\{h0l\}$  indicate as probable space groups  $Pna2_1$  ( $C_{2v}^2$ ) and  $Pnam$  ( $D_{2h}^{10}$ ).

The disposition of the lead atoms is consistent with both space groups.

If the space group is  $Pnam$  the asymmetric unit contains only half a formula unit since there are only four  $\text{Pb}(\text{C}_5\text{H}_5)_2$  per unit cell: the two cyclopentadienyl groups must be mirrored across the plane  $z/c=0.25$  on which the crystallographically independent lead atom lies. Since the symmetry requirements of the non-centrosymmetric space group  $Pna2_1$  do not specify the origin of the unit cell in the  $c$  lattice vector direction, the  $z/c$  coordinate of the independent lead atom can be arbitrarily chosen as 0.25.

From Patterson [001] and [010] projections, it was possible to determine the positions of the independent lead atom at  $x/a=0.0821$ ,  $y/b=0.1050$ ,  $z/c=0.2500$ . Two Fourier syntheses based on  $Pnam$  were calculated with the signs given by the heavy atom. The coordinates of the maxima of electron density on the [010] map around the lead atom require a cyclopentadienyl ring across the symmetry plane  $z/c=0.25$  with a second cyclopentadienyl ring positioned about the origin of the unit cell. Hence, the centrosymmetric space group  $Pnam$  can be ruled out, since it contains a centre of symmetry at the origin, which would allow a cyclopentadienyl ring about it only if the structure were disordered. Since images of the cyclopentadienyl rings were generated phased on the centrosymmetrically located lead atoms, the non-centrosymmetric space group  $Pna2_1$  was chosen as the correct one. Fig. 1 shows the positions of the cyclopentadienyl rings based on the interpretation of the Fourier maps.

The coordinates of the cyclopentadienyl rings were refined by the difference synthesis method. The unweighted reliability index for the  $\{h0l\}$  and  $\{hk0\}$  data decreased from 0.13 and 0.18 respectively to 0.08 and 0.10. With the use of anisotropic temperature coefficients for the lead atom and an identical isotropic factor for the carbon

Table 1. Atomic coordinates and isotropic temperature factors

	$x/a$	$\sigma(x/a)$	$y/b$	$\sigma(y/b)$	$z/c$	$\sigma(z/c)$	$B(hk0)$	$B(h0l)$
Pb	0.0818 +	0.0003	0.1030 +	0.0007	0.2500 +	0.0004	*	*
C(1)	0.4418 +	0.004	0.4366 +	0.004	0.0433 +	0.004	1.50	3.46
C(2)	0.4968 +	0.004	0.3000 +	0.004	0.0267 -	0.004	1.50	3.46
C(3)	0.5651 +	0.004	0.3900 +	0.002	0.0733 -	0.004	1.50	3.46
C(4)	0.5484 +	0.004	0.6300 +	0.002	0.0267 -	0.007	1.50	3.46
C(5)	0.4801 +	0.003	0.6433 +	0.002	0.0400 +	0.006	1.50	3.46
C(6)	0.1900 +	0.004	0.4233 +	0.004	0.3533 +	0.002	1.50	3.46
C(7)	0.1984 +	0.004	0.4433 +	0.004	0.2066 +	0.002	1.50	3.46
C(8)	0.2334 +	0.004	0.2466 +	0.004	0.1400 +	0.004	1.50	3.46
C(9)	0.2500 +	0.002	0.1233 +	0.003	0.2366 +	0.005	1.50	3.46
C(10)	0.2217 +	0.002	0.2000 +	0.003	0.3600 +	0.004	1.50	3.46

\* For the lead atom the anisotropic thermal parameters are of the form  $\exp \left\{ -0.25 \sum_{i=1}^3 \sum_{j=1}^3 B_{ij} h_i h_j a_i^* a_j^* \right\}$

$\{hk0\}$ :  $B_{11}=2.06$ ;  $B_{12}=-0.19$ ;  $B_{22}=3.94$ .  $\{h0l\}$ :  $B_{11}=3.20$ ;  $B_{13}=0.00$ ;  $B_{33}=4.42$

Table 2. Bond lengths

Pb(1)-C(1)	3.041 Å	Pb(1)-C(6)	2.799 Å	C(1)-C(2)	1.392 Å	C(6)-C(7)	1.420 Å
Pb(1)-C(2)	3.055	Pb(1)-C(7)	2.830	C(2)-C(3)	1.320	C(7)-C(8)	1.462
Pb(1)-C(3)	3.116	Pb(1)-C(8)	2.832	C(3)-C(4)	1.536	C(8)-C(9)	1.218
Pb(1)-C(4)	3.053	Pb(1)-C(9)	2.761	C(4)-C(5)	1.291	C(9)-C(10)	1.354
Pb(1)-C(5)	3.006	Pb(1)-C(10)	2.589	C(5)-C(1)	1.393	C(10)-C(6)	1.442
Pb(2)-C(1)	3.014						
Pb(2)-C(2)	3.095	Average	2.762	Average C-C	1.386	Average C-C	1.379
Pb(2)-C(3)	3.210						
Pb(2)-C(4)	3.028	Pb(1)-Pb(2)	5.636				
Pb(2)-C(5)	2.973						

Average Pb-C 3.059

atoms, the intensity data were further refined to final discrepancy values of 0.065 for  $\{h0l\}$  and 0.064 for  $\{hk0\}$ .

Atomic form factors were calculated by the method of Vand, Eiland & Pepinski (1957) and the subsequent modifications of Forsyth & Wells (1959). The other crystallographic programs utilized in the structural analysis were written by Panattoni & Frasson (1962) for Olivetti Elea 6001 computers.

The accuracy of the proposed coordinates was calculated by the method of Cruickshank (1949). Standard deviations were calculated for the well-resolved atoms; no estimates were made for overlapping carbon atoms for which it was

Table 3. Observed and calculated structure factors ( $\times 10$ )

Unobserved reflexions for which  $10F_o$  is listed as 0 have  $10F_c < 300$

$hk\bar{0}$					$h\bar{0}l$					
$h$	$F_o$	$F_c$	$h$	$F_o$	$F_c$	$h$	$F_o$	$F_c$	$A_c$	$B_c$
k=0										
2	1570	1558	167	630	634	2	249	234	142	142
4	2731	2777	548	1139	1157	4	447	445	281	281
6	3146	3142	0	1833	1833	6	645	645	420	420
8	3594	3594	0	2527	2527	8	843	843	559	559
10	4077	4077	0	3221	3221	10	1041	1041	698	698
12	4594	4594	0	3915	3915	12	1239	1239	837	837
14	5147	5147	0	4609	4609	14	1437	1437	976	976
16	5736	5736	0	5303	5303	16	1635	1635	1115	1115
18	6363	6363	0	6000	6000	18	1833	1833	1254	1254
20	7038	7038	0	6700	6700	20	2031	2031	1393	1393
22	7763	7763	0	7400	7400	22	2229	2229	1532	1532
24	8538	8538	0	8100	8100	24	2427	2427	1671	1671
26	9363	9363	0	8800	8800	26	2625	2625	1810	1810
28	10238	10238	0	9500	9500	28	2823	2823	1949	1949
30	11163	11163	0	10200	10200	30	3021	3021	2088	2088
32	12138	12138	0	10900	10900	32	3219	3219	2227	2227
34	13163	13163	0	11600	11600	34	3417	3417	2366	2366
36	14238	14238	0	12300	12300	36	3615	3615	2505	2505
38	15363	15363	0	13000	13000	38	3813	3813	2644	2644
40	16538	16538	0	13700	13700	40	4011	4011	2783	2783
42	17763	17763	0	14400	14400	42	4209	4209	2922	2922
44	19038	19038	0	15100	15100	44	4407	4407	3061	3061
46	20363	20363	0	15800	15800	46	4605	4605	3200	3200
48	21738	21738	0	16500	16500	48	4803	4803	3339	3339
50	23163	23163	0	17200	17200	50	5001	5001	3478	3478
52	24638	24638	0	17900	17900	52	5199	5199	3617	3617
54	26163	26163	0	18600	18600	54	5397	5397	3756	3756
56	27738	27738	0	19300	19300	56	5595	5595	3895	3895
58	29363	29363	0	20000	20000	58	5793	5793	4034	4034
60	31038	31038	0	20700	20700	60	5991	5991	4173	4173
62	32763	32763	0	21400	21400	62	6189	6189	4312	4312
64	34538	34538	0	22100	22100	64	6387	6387	4451	4451
66	36363	36363	0	22800	22800	66	6585	6585	4590	4590
68	38238	38238	0	23500	23500	68	6783	6783	4729	4729
70	40163	40163	0	24200	24200	70	6981	6981	4868	4868
72	42138	42138	0	24900	24900	72	7179	7179	5007	5007
74	44163	44163	0	25600	25600	74	7377	7377	5146	5146
76	46238	46238	0	26300	26300	76	7575	7575	5285	5285
78	48363	48363	0	27000	27000	78	7773	7773	5424	5424
80	50538	50538	0	27700	27700	80	7971	7971	5563	5563
82	52763	52763	0	28400	28400	82	8169	8169	5702	5702
84	55038	55038	0	29100	29100	84	8367	8367	5841	5841
86	57363	57363	0	29800	29800	86	8565	8565	5980	5980
88	59738	59738	0	30500	30500	88	8763	8763	6119	6119
90	62163	62163	0	31200	31200	90	8961	8961	6258	6258
92	64638	64638	0	31900	31900	92	9159	9159	6397	6397
94	67163	67163	0	32600	32600	94	9357	9357	6536	6536
96	69738	69738	0	33300	33300	96	9555	9555	6675	6675
98	72363	72363	0	34000	34000	98	9753	9753	6814	6814
100	75038	75038	0	34700	34700	100	9951	9951	6953	6953
102	77763	77763	0	35400	35400	102	10149	10149	7092	7092
104	80538	80538	0	36100	36100	104	10347	10347	7231	7231
106	83363	83363	0	36800	36800	106	10545	10545	7370	7370
108	86238	86238	0	37500	37500	108	10743	10743	7509	7509
110	89163	89163	0	38200	38200	110	10941	10941	7648	7648
112	92138	92138	0	38900	38900	112	11139	11139	7787	7787
114	95163	95163	0	39600	39600	114	11337	11337	7926	7926
116	98238	98238	0	40300	40300	116	11535	11535	8065	8065
118	101363	101363	0	41000	41000	118	11733	11733	8204	8204
120	104538	104538	0	41700	41700	120	11931	11931	8343	8343
122	107763	107763	0	42400	42400	122	12129	12129	8482	8482
124	111038	111038	0	43100	43100	124	12327	12327	8621	8621
126	114363	114363	0	43800	43800	126	12525	12525	8760	8760
128	117738	117738	0	44500	44500	128	12723	12723	8899	8899
130	121163	121163	0	45200	45200	130	12921	12921	9038	9038
132	124638	124638	0	45900	45900	132	13119	13119	9177	9177
134	128163	128163	0	46600	46600	134	13317	13317	9316	9316
136	131738	131738	0	47300	47300	136	13515	13515	9455	9455
138	135363	135363	0	48000	48000	138	13713	13713	9594	9594
140	139038	139038	0	48700	48700	140	13911	13911	9733	9733
142	142763	142763	0	49400	49400	142	14109	14109	9872	9872
144	146538	146538	0	50100	50100	144	14307	14307	10011	10011
146	150363	150363	0	50800	50800	146	14505	14505	10150	10150
148	154238	154238	0	51500	51500	148	14703	14703	10289	10289
150	158163	158163	0	52200	52200	150	14901	14901	10428	10428
152	162138	162138	0	52900	52900	152	15099	15099	10567	10567
154	166163	166163	0	53600	53600	154	15297	15297	10706	10706
156	170238	170238	0	54300	54300	156	15495	15495	10845	10845
158	174363	174363	0	55000	55000	158	15693	15693	10984	10984
160	178538	178538	0	55700	55700	160	15891	15891	11123	11123
162	182763	182763	0	56400	56400	162	16089	16089	11262	11262
164	187038	187038	0	57100	57100	164	16287	16287	11401	11401
166	191363	191363	0	57800	57800	166	16485	16485	11540	11540
168	195738	195738	0	58500	58500	168	16683	16683	11679	11679
170	200163	200163	0	59200	59200	170	16881	16881	11818	11818
172	204638	204638	0	59900	59900	172	17079	17079	11957	11957
174	209163	209163	0	60600	60600	174	17277	17277	12096	12096
176	213738	213738	0	61300	61300	176	17475	17475	12235	12235
178	218363	218363	0	62000	62000	178	17673	17673	12374	12374
180	223038	223038	0	62700	62700	180	17871	17871	12513	12513
182	227763	227763	0	63400	63400	182	18069	18069	12652	12652
184	232538	232538	0	64100	64100	184	18267	18267	12791	12791
186	237363	237363	0	64800	64800	186	18465	18465	12930	12930
188	242238	242238	0	65500	65500	188	18663	18663	13069	13069
190	247163	247163	0	66200	66200	190	18861	18861	13208	13208
192	252138	252138	0	66900	66900	192	19059	19059	13347	13347
194	257163	257163	0	67600	67600	194	19257	19257	13486	13486
196	262238	262238	0	68300	68300	196	19455	19455	13625	13625
198	267363	267363	0	69000	69000	198	19653	19653	13764	13764
200	272538	272538	0	69700	69700	200	19851	19851	13903	13903
202	277763	277763	0	70400	70400	202	20049	20049	14042	14042
204	283038	283038	0	71100	71100	204	20247	20247	14181	14181
206	288363	288363	0	71800	71800	206	20445	20445	14320	14320
208	293738	293738	0	72500	72500	208	20643	20643	14459	14459
210	299163	299163	0	73200	73200	210	20841	20841	14598	14598
212	304638	304638	0	73900	73900	212	21039	21039	14737	14737
214	310163	310163	0	74600	74600	214	21237	21237	14876	14876
216	315738	315738	0	75300	75300	216	21435	21435	15015	15015
218	321363	321363	0	76000	76000	218	21633	21633	15154	15154
220	327038	327038	0	76700	76700	220	21831	21831	15293	15293
222	332763	332763	0	77400	77400	222	22029	22029	15432	15432
224	338538	338538	0	78100	78100	224	22227	22227	15571	15571

The  $p_z$  orbitals for the lead atoms and one of the  $e_1$  orbitals of the cyclopentadienyl ring (with the right symmetry) are arranged in such a way as to give a conjugated system. A monomeric molecule participates in the  $\pi$  system with four electrons.

This configuration justifies a planar structure for the polymeric chain.

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**Intensity corrections for the Guinier camera.** By W. H. SAS and P. M. DE WOLFF, *Laboratorium voor Technische Natuurkunde der Technische Hogeschool, Lorentzweg 1, Delft, The Netherlands*

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#### Intensity corrections for the Guinier camera

The integrated intensities as measured on a photometer record of powder diffraction lines on a Guinier film can be written as follows:

$$I = kpTF^2LPABSG; L = 1/\sin^2 \theta \cos \theta \quad (1)$$

where  $k$ ,  $p$ ,  $T$ ,  $F$ ,  $L$  and  $P$  are scale-, multiplicity-, temperature-, structure-, Lorentz- and polarization factor respectively. We shall show that the combined effect of the remaining factors  $A, B, S, G$  can be approximated by a linear function of  $\cos(2\theta - \psi)$ ,  $\psi$  being the angle between specimen normal and crystal-reflected primary beam; and we present nomograms from which the normalized slope of this function can be found for  $\psi = 30^\circ$ .

The factor  $A$  accounts for absorption in the specimen (thickness  $d$ , linear absorption coefficient  $\mu$ ):

$$A = \frac{1}{\mu d} \frac{\cos \psi \cdot \cos \chi}{\cos \psi - \cos \chi} [\exp \{-(\mu d / \cos \psi)\} - \exp \{-(\mu d / \cos \chi)\}] \quad (2)$$

where  $\chi = |2\theta - \psi|$ .

The factor  $B$  accounts for absorption in a layer which is often present in front of the film, e.g. wrapping paper or filter (thickness  $d_p$ , linear absorption coefficient  $\mu_p$ ).

$$B = \exp \{-(\mu_p d_p / \cos \chi)\} \quad (3)$$

$S$  is the oblique incidence factor for integrated intensities:

$$S = \frac{[1 - \exp \{-(\mu_1 d_1 / \cos \chi)\}]}{[1 - \exp \{-\mu_1 d_1\}]} \times \frac{[1 + \exp \{-(\mu_1 d_1 + \mu_2 d_2) / \cos \chi\}]}{[1 + \exp \{-(\mu_1 d_1 + \mu_2 d_2)\}]} \quad (4)$$

where  $d_1$  and  $d_2$  are the thicknesses of one layer of emulsion and of the base, respectively and  $\mu_1, \mu_2$  are the corresponding linear absorption coefficients (*International Tables for X-ray Crystallography*, 1962).  $G$  is a geometric factor:

$$G = 1/\cos \chi \quad (5)$$

(*International Tables*, 1962), arising from the fact that the  $\theta$ -dependent factor in (1) is valid for a constant specimen-film distance, whereas in the Guinier camera that distance varies as  $\cos \chi$ . Since a photometer measures the energy over a constant height of the diffraction line, the corresponding fraction of the total energy in the Debye-Scherrer cone contains the extra factor  $1/\cos \chi$ .\*

If we define  $N = A B S G$ , then  $N$  is a function of  $\cos \chi$ , with parameters  $\psi, \mu d, \mu_1 d_1, \mu_2 d_2, \mu_p d_p$ , because  $A, B, S, G$  are all functions of  $\cos \chi$ . For  $\mu_1 d_1 = \mu_2 d_2$  as well as for  $\mu_2 d_2 = 0$  and a great number of different combinations of

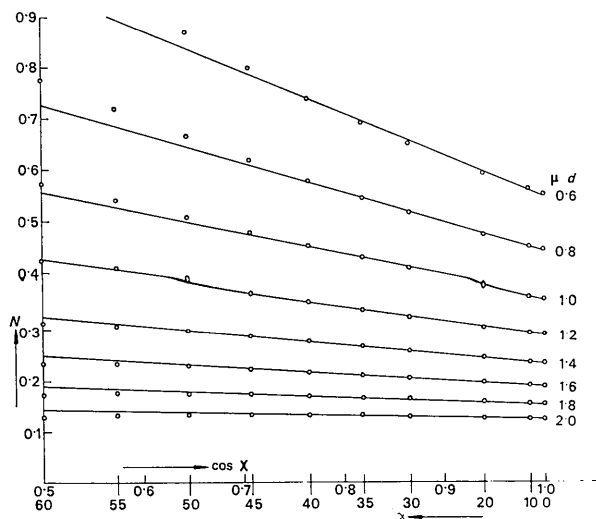


Fig. 1. The combined correction factor  $N = A B S G$  (circles) as a function of  $\cos \chi$  for  $\psi = 30^\circ$ ,  $\mu_1 d_1 = \mu_2 d_2 = 0.35$ ,  $\mu_p d_p = 0.1$  and 8 values of  $\mu d$ . The linear least-squares approximation is shown by the straight lines.

\* Hellner (1954) gave an entirely different expression for the geometric factor, which has been cited and tabulated by Sagel (1958). Professor Hellner (private communication) now states that his formula resulted from an erroneous derivation and kindly pointed out to us that the correct expression was given first by Hägg & Regnström (1944).